## Technical Math - Master Rubric

| Competency and Indicator | Level 1 - No Evidence | Level 2 - Partially Meets | Level 3 - Approaches | Level 4 - Meets | Level 5 - Exceeds |
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|  | Student does not meet prerequisite skills. | Student demonstrates prerequisite skills. | Student demonstrates understanding of simple indicators. | Student demonstrates understanding of complex indicators in an authentic task. | Student demonstrates understanding of indicators that goes beyond expectations. |
| TM-NS1.A. Analyze proportional relationships and use them to solve contextualized and mathematical problems. | A. Not yet able to setup a ratio or proportion. | A. Set up a single ratio using units. | A. Set up a proportion and solve. | A. Set-up and solve a proportion as part of an authentic task. <br> Including units when applicable. <br> AND <br> A. Describe the proportional relationship between quantities within an authentic task. | A. Create equivalent proportions for quantities with an authentic task. |
| TM-NS1.B. Compute unit rates associated with ratios of fractions, decimals, and percent and including ratios of lengths, areas and other quantities measured in like or different units. | B. Not yet able to calculate rates. | B. Calculate unit rates of like units of quantities. | B. Calculate unit rates from like and unlike units of quantities. | B. Calculate unit rates from like and unlike units of quantities given within an authentic task. | B. Find and correct calculation errors within an authentic task. |
| TM-NS1.C. Apply properties of operations to calculate with numbers in any form | C. Not yet able to consistently calculate answers for problems using real numbers in an authentic task. | C. Calculate values for different problems within an authentic task(s) for an integer. | C. Calculate values for different problems within an authentic task(s) for integer, simple fractions and simple decimal. | C. Calculate values for different problems within an authentic task(s) for any real number. Problems must include signed | C. Find and correct calculation errors, using any real number, within an authentic task. |


| including signed numbers. |  |  |  | values and a variety of real numbers. |  |
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| TM-NS1.D. Convert between forms as appropriate. | D. Not yet able to convert between decimal, common fractions, and percentages. | D. Convert between two forms. (ie fraction to decimal only) | D. Convert between decimal, common fractions, and percentages. | D. Convert between decimal, common fractions, and percentages within an authentic task. | D. Convert between decimal, common fractions, and percentages using mental math. |
| TM-NS1.E. Assess the reasonableness of answers using mental computation and estimation and rounding strategies. | E. Not yet able to use mental math skills to determine if an answer is reasonable. | E. Apply basic rules of rounding and estimation using mental math. | E. Recognize reasonable solutions to problem and level of needed precision. | E. Mathematically determine and support, using mental math, the reasonableness of an answer to a contextual problem. (Must be able to determine and support reasonable and non-reasonable answers.) | E. Apply mental math skills to find and correct errors in contextual problems. |
| TM-NS1.F. Use <br> rational approximations of irrational numbers to compare the size of irrational numbers and estimate the value of expressions (e.g., $\pi / 2$ ). | F. Not yet able to calculate rational approximations. | F. Determine placement on a number line between consecutive integers. | F. Estimate approximations of irrational numbers and be able to round up to next larger integer to estimate values with in an authentic task. | F. Apply rational approximations to more precisely estimate values within an authentic task. | F. Apply multiple rational approximations within one task to more precisely estimate values. |
| TM-NS2.A. Convert like measurement units within a given measurement system and between systems. | A. Not yet able to convert units between like or unlike systems. | A. Convert units within the same measurement system. (ie converting inches to feet, centimeters to meters) | A. Convert units between measurement systems. | A. Convert units within a measurement system and between systems within an authentic task. | A. Accurately convert units among and between systems and determine which system is more applicable to the given scenario. |
| TM-NS2.B. Convert among different sized standard and/or metric measurement units and use these conversions in solving | B. Not yet able to convert different sized units between like or unlike systems within an authentic task. | B. Recognize <br> measurement system and measurement units are appropriate to use within an authentic | B. Convert different sized units between like systems from an authentic task. | B. Convert different sized units within a measurement system and between systems within an authentic task. | B. Accurately convert units among and between systems and determine which system and/or unit is |


| authentic multi-step problems. |  | task and can develop a plan for solving. |  |  | more applicable to the given scenario. |
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| TM-NS2.C. Use ratio reasoning (dimensional analysis) to convert measurement units including, but not limited to, distances and rates. | C. Not yet able to convert measurement units within a ratio. | C. Recognize which ratio must be used to convert to measurement. | C. Apply dimensional analysis to convert a measurement | C. Apply dimensional analysis to convert units, including distance and rates, within an authentic task. | C. FInd and correct an error within an authentic task. <br> C. Apply multiple ratios to solve an authentic task. |
| TM-NS2.D. <br> Manipulate and transform units appropriately when multiplying or dividing quantities. <br> ie $\mathrm{ft} \mathbf{X f t}$ is $\mathrm{ft}^{\wedge} \mathbf{2}$, ft per second divided by feet yields seconds | D. Not yet able to manipulate and transform units when multiplying or dividing quantities with units. | D. Recognize which units must be used when multiplying or dividing quantities with units with initial units and ending units. | D. Manipulate and transform units when multiplying and dividing quantities with units. | D. Manipulate and transform units when multiplying and dividing quantities with units in an authentic task. | D. Find and correct a unit error within an authentic task. |
| TM-NS3.A. Evaluate expressions at specific values for their variables. Include expressions that arise from formulas in authentic problems. | A. Not yet able to accurately evaluate an expression for a given value. | A. Evaluate variable expressions with integer values. | A. Evaluate variable expressions with integers, decimals, and fraction values. | A. Evaluate variable expressions containing common integer, decimal, and fractional values found in authentic task. (with and without technology) | A. Explain how the values of the variable(s) effect with each other and how changes can affect the final value in an authentic task. |
| TM-NS3.B. Perform arithmetic operations, including those involving wholenumber exponents, | B. Not yet able to apply order of operations. | B. Explain the process using the order of operations to simplify a given expression. | B. Use order of operations to simplify an expression. | B. Calculate an order of operation problem with an authentic task which involves whole number | B. Find and correct an error with an order of operation problem which includes whole number exponents. |


| using order of operations. |  |  |  | exponents. (with and without technology) <br> AND <br> B. Explain the process used to calculate and order of operation problem within an authentic task which includes whole number exponents. |  |
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| TM-NS3.C. Work with radicals and integer exponents. | C. Not yet able to simplify a problem with radical or integer exponents. | C. Able to compute with radicals and integer exponents on a calculator. | C. Evaluate formulas with radicals and integer exponents. | C. Solve problems or use formulas within an authentic task which involve radical and integer exponents. | C. Find and correct an error within a problem which includes radical and integer exponents. |
| TM-NS3.D. Use square root and cube root symbols to represent solutions to equations of the form $x^{2}=p$ and $x^{3}=p$, where $p$ is a positive rational number. | D. Not yet able to use root symbols to represent solutions to equations. | D. Recognize that $x$ is a square root or cube root of $p$, where $p$ is a positive rational number | D. Correctly using the square root and cube root symbols in the solutions to $x^{2}=p$ and $x^{3}=p$, where $p$ is a positive rational number | D. Correctly using the square root and cube root symbols in the solutions to $x^{2}=p$ and $x^{3}=p$, where $p$ is a positive rational number, within an authentic task. | D. Develop an algebraic expression that demonstrates the transition from exponents to radical solutions within an authentic task |
| TM-NS3.E. Evaluate square roots of small (1-12) perfect squares and cube roots of small(1-5) perfect cubes. | E. Not yet able to evaluate perfect square or cube root. | E. Recognize perfect squares and perfect cubes. | E. Evaluate small, perfect square and cube roots with a calculator. | E. Evaluate small, perfect square and cube roots, within an authentic task without a calculator. | E. Evaluate larger perfect square and cube roots within an authentic task without a calculator. |
| TM-NS3.F. Know that square roots and cubed roots of nonperfect squares and cubes are irrational and understand what | F. Not yet able to make a connection between a non-perfect square or cube root and an irrational number. | F. Estimate roots of non-perfect squares and cubes using a calculator. | F. Recognize a value as an estimate (close in value) of a non-perfect square or cube. | F. Estimate the value of a non-perfect square or cube root when solving problems. <br> AND | F. Estimate values of a non-perfect square or cube root without technology and determine how to use |


| irrational numbers are. |  |  |  | F. Determine when an answer in an authentic task will be an irrational number. Can describe how accuracy is impacted by the use of irrational numbers. | the value in context of the authentic task. |
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| TM-NS4.A. Draw conclusions and justify those conclusions from graphics such as order forms, bar charts, pie charts, diagrams, flow charts, maps, and dashboards. | A. Not yet able to make conclusions from different types of visual representation of data. | A. Can identify what the parts of the graph represent of various representations. (such as horizontal and vertical axis) | A. Can estimate values to make conclusions from a variety of visual representations. | A. Make and justify conclusions made from different types of visual representations of data within an authentic task. | A. Justify a different conclusion, based on the same data sets, within an authentic task. |
| TM-NS4.B. Identify and interpret trends, patterns, and relationships from graphs and charts. | B. Not yet able to interpret trends, patterns or relationships from graphs and charts. | B. Identify differences, general characteristics, or trends of graphs. (ie such as size of value or increasing vs. decreasing) | B. Can compare and state differences, general characteristics, or trends of graphs | B. Identify and interpret trends, patterns, and relationships from graphs and charts in an authentic situation. | B. Use trends to make predictions based on the identification and interpretation of trends and patterns in an authentic task. |
| TM-NS4.C. Identify types of graphs that best represent a given set of data. | C. Not yet able to identify graphs and uses for them. | C. Identify types of graphs and what they are used for. | C. Recognize when specific data is best represented by certain graphs | C. Identify and defend chosen graphical representation of a given set of data from an authentic task. | C. Identify pros and cons of different graphs given a set of data from an authentic task. |
| TM-NS4.D. Make and justify decisions based on data. | D. Not yet able to make a decision without guided support or examples. | D. Make a decision while solving an authentic task, may be a correct or incorrect decision. | D. Make a decision and recite the process used to make a decision when solving an authentic task. | D. Explain and justify, using data and information as support, a decision made while solving an authentic task. | D. Critique another person's decision and process used. |
| TN-G1.A. Use perimeter, area, and volume formulas to calculate | A. Not yet able to use formulas to calculate measurements of a figure. | A. Identify which formula and units are appropriate for | A. Determine measurements of figures using formulas | A. Determine measurements of figures using geometric formulas of perimeter, | A. Determine ideal (optimal) measurements of a |


| measurements of geometric figures. |  | calculating measurements. | of perimeter, area, and volume. | area, and volume within an authentic task. | figure within an authentic task. |
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| TM-G2.A. Use facts about supplementary, complementary, vertical, adjacent, corresponding, alternate interior, and alternate exterior angles to solve for an unknown angle. | A. Not yet able to apply angle properties to determine unknown angle measures within an authentic figure. | A. Recognize supplementary, complementary, vertical, adjacent, and corresponding angles on authentic figure. | A. Apply angle properties, such as vertical angles are congruent, to calculate unknown angle values. | A. Determine unknown angle measures within an authentic task applying angle properties. | A. Explain the properties being used to solve for missing angle measures in an authentic task. |
| TM-G2.B. Accurately measure parts of geometric figures such as sides, perimeter, circumference, diagonals, diameter, and angles using the correct measurement tool. | B. Not yet able to correctly use a measurement tool to find the measure of geometric figures. | B. Recognize which measuring instrument and units are appropriate. | B. Measure and write the measurement of figures on paper. | B. Measure and write the measurement of part(s) of real world geometric figures using correct tool. | B. Measure and write the measurement of part(s) of real world geometric compound figures using correct tool. |
| TM-G2.C. Solve problems involving scale drawings of geometric figures including computing actual lengths and areas from a scale drawing and reproducing a scale drawing at a different scale. | C. Not yet able to apply scale drawings to compute actual measurements. | C. Identify given scale and convert length to actual units. | C. Create a drawing using a given scale. <br> (Can be a simple object from classroom or can use technology if school has access.) | C. Reproduce a scale drawing applying a different scale. <br> AND <br> C. Solve a variety of problems involving scale drawings within an authentic task. | C. Adjust <br> measurements within a scale drawing to give different options to an authentic task. |
| TM-G2.D. Represent applied problems by graphing points in the coordinate plane and interpret coordinate | D. Not yet able to recognize coordinates of points or graph points | D. Can graph points and give coordinates of points on a graph. | D. Graph contextual situation on a coordinate plane with a given labeled axis. | D. Graph and interpret meanings of coordinate points from an authentic task with given origin and scale. | D. Create the graph and label axis, scale, coordinates from an authentic task. |


| values of points in the context of the situation. |  |  |  |  |  |
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| TM-G3.A. Use the Pythagorean <br> Theorem to solve for the length of a leg or the hypotenuse of right triangles. | A. Not yet able to apply Pythagorean Theorem to calculate an unknown side of a triangle. | A. Identify the legs and hypotenuse of a right triangle. | A. Apply the Pythagorean Theorem to find sides of a right triangle. | A. Apply Pythagorean Theorem in an authentic task to find the side of a right triangle. | A. Apply Pythagorean Theorem in an authentic task to determine if the measures form an acute, right, or obtuse triangle. |
| TM-G3.B. Use right triangle ratios (sine, cosine, tangent, and their inverses) to solve for unknown sides and angles in right triangles. | B. Not yet able to apply right triangle trigonometry to calculate unknown sides and angles in a right triangle. | B. Can find trigonometry ratios of an acute angle of a triangle with known sides. | B. Calculate unknown sides and angles of a right triangles. | B. Calculate unknown sides and angles of a right triangles within an authentic task. | B. Prove calculations using a different Trigonometry function or another Triangle Property. (ie Triangle Sum and Pythagorean Theorem) |
| TM-BA1.A. Use properties of operations to generate equivalent expressions. | A. Not yet able to create equivalent expressions. | A. Identify equivalent expressions. | A. Show that two expressions are equivalent. | A. Apply properties of operations to create equivalent expressions within an authentic task. | A. Describe properties and operations to create equivalent expressions within an authentic task. |
| TM-BA1.B. Apply properties of operations as strategies to add, subtract, factor, and expand linear expressions with rational coefficients. | B. Not yet able to apply properties of operations with expressions containing rational coefficients. | B. Able to add, subtract, factor linear expressions with integers. | B. Able to add, subtract, and factor linear expressions with rational numbers. | B. Add, subtract, factor, and expand linear expressions with rational coefficients within an authentic task. | B. Find and correct an error when adding, subtracting, factoring and expanding a linear expression within an authentic task. |
| TM-BA1.C. Solve linear equations and inequalities in one variable. | C. Not yet able to solve single variable equations and inequalities. | C. Solve two-step equation and inequality. | C. Solve multi-step equations and inequalities. | C. Solve and interpret solution of linear equations and inequalities, in one | C. Find and correct solution errors and/or interpretation errors of equations or |


|  |  |  |  | variable, within an authentic task. | inequalities within an authentic task. |
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| TM-BA1.D. Use linear equations to model authentic contexts. | D. Not yet able to model an authentic task with a linear equation. | D. Define variable and restate known values from an authentic task. | D. Model an authentic task with a linear equation, may be incorrect. | D. Model an authentic task with linear equations. Defining variable(s) and solution meaning within context of the task. | D. Model, solve, and interpret solution(s) of linear equations within an authentic task. |
| TM-BA2.A. Use variables to represent two quantities involving geometric figures that change in relationship to one another. | A. Not yet able to represent two quantities of a figure as variables. | A. Define quantities needed given a geometric formula. | A. Evaluate the geometric relationship with different values in the two quantities and note changes in one quantity when the other is changed. | A. Define and use variables that represent quantities of geometric figures within an authentic task. <br> AND <br> A. Describe the relationship of two quantities within a geometric figure and how they change in relationship to each other. | A. Predict the impact of change on one variable as it relates to the second variable, using an authentic task. |
| TM-BA2.B. Write an equation to express one quantity, thought of as the dependent variable, in terms of the other quantity, thought of as the independent variable. | B. Not yet able to write an equation with an independent and dependent variable that represents an authentic task. | B. Identify the dependent and independent variables in an equation. | B. Write an equation for one variable in terms of another. | B. Write and define an equation that represents an authentic task having an independent and dependent variable. | B. Describe the relationship, using explicit terms, values, or units, of the two variables in an authentic task. |
| TM-BA2.C. Rearrange formulas to highlight a quantity of interest using the same reasoning as in solving equations. | C. Not yet able to solve a literal equation. | C. Solve 1 or 2 step literal equations. | C. Solve multi-step literal equations. | C. Solve and interpret a formula (literal equation) within an authentic task. | C. Explain effects to the formula as changes to a variable happen within an authentic task. |


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| TM-BA3.A. Evaluate <br> expressions, including <br> those that arise from <br> formulas in authentic <br> problems, at specific <br> values for their <br> variables. | A. Not yet able to <br> evaluate an expression. | A. Correctly substitute <br> the numbers into the <br> expression. | A. Evaluate the <br> expression or formula, <br> with correct units. | A. Evaluate the <br> expression or formula, <br> with correct units, <br> within an authentic <br> task. | A. Explain answers from <br> an authentic task. |
| TM-BA3.B. Reason <br> quantitatively and use <br> units to solve <br> problems as a way to <br> understand problems <br> and to guide the <br> solution of multi-step <br> problems. | B. Not yet able to apply <br> units to reason <br> quantitatively about a <br> problem. | B. Compare different <br> quantities based on <br> units to decide steps <br> for solving a problem. | B. Apply quantitative <br> reasoning when solving <br> a simple task. | B. Apply quantitative <br> reasoning when solving <br> a multi-step problem <br> within an authentic <br> task. | B. Explain and defend a <br> multi-step solution <br> within an authentic <br> task using quantitative <br> reasoning. |
| TM-BA3.C. Choose and <br> interpret units <br> consistently in <br> formulas. | C. Not yet able to <br> choose units of <br> measure in formulas. | C. Determine <br> appropriate units for <br> final answers. | C. Recognize different <br> unit measures within a <br> problem and convert <br> correctly. | C. Interpret units of <br> measure in a formula <br> within an authentic <br> task. | C. Justify final unit <br> measure selection. |
| TM-BA3.D. Apply <br> appropriate formulas <br> to solve applications. | D. Not yet able to apply <br> formulas within an <br> authentic task. | D. Determine correct <br> formula for an <br> authentic task when <br> given options. | D. Select the <br> appropriate formula to <br> solve an authentic task. | D. Select and apply <br> appropriate formulas to <br> solve problems in an <br> authentic task. | D. Apply and explain <br> formulas used to solve <br> problems in an <br> authentic task. |

